

# Egzamin pisemny z Mechaniki Konstrukcji II, 11 IX 2023 r.

NAZWISKO imię

## Zadanie 1

Masa danej ramy jest skoncentrowana w dwu węzłach.

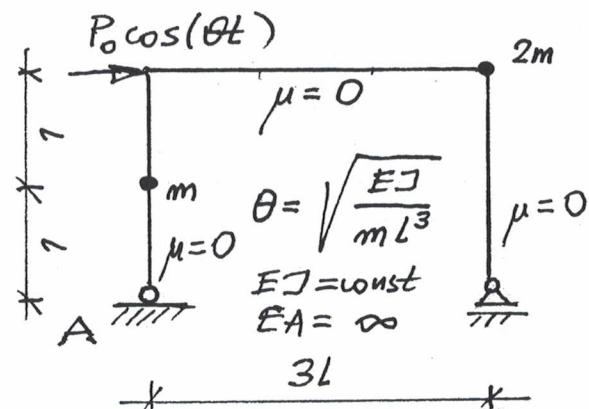
Rama jest poddana obciążeniu harmonicznemu jak na rysunku.

Zapisać równania określające amplitudę reakcji poziomej w podporze A.

(The mass of the given frame is concentrated at two nodes.

The frame is subject to the harmonic load, see the figure.

Write down the equations which make it possible to compute the amplitude of the horizontal reaction at the support A.)



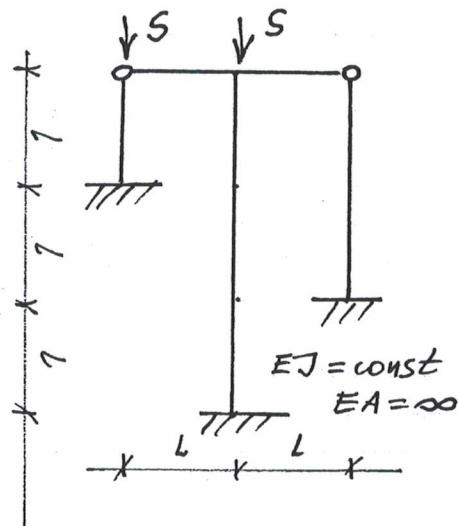
## Zadanie 2

Dana jest rama płaska obciążona Dużymi siłami osiowymi jak na rys.

Zapisać równania utraty stateczności całej ramy.

(Given is the frame subject to big axial forces, see the figure.

Write down the equations expressing the loss of stability of equilibrium of the whole frame).



## Zadanie 3

Dana jest rama jak na rysunku.

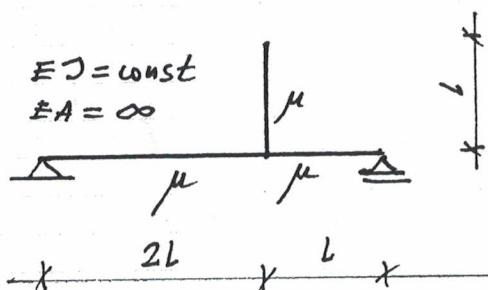
Zapisać równania określające

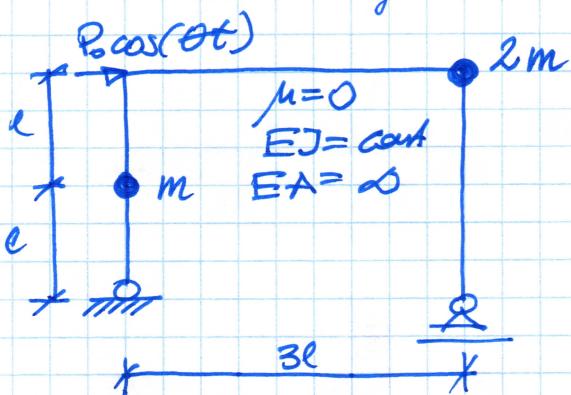
pierwszą częstotliwość drgań własnych.

(Given is a frame, cf. the figure.

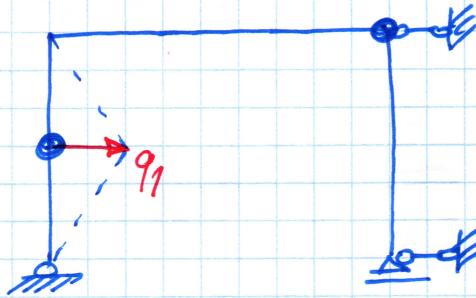
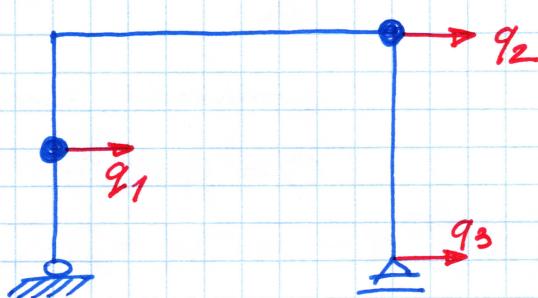
Write down the equations which determine

the first circular frequency)





$$\theta = \sqrt{\frac{EJ}{ml^3}}$$



$q_1, q_2$  - dynamiczne stopnie swobody  
 $q_3$  - statyczny stopień swobody

$$q_f = \begin{bmatrix} q_1 \\ q_2 \end{bmatrix}$$

$$E_k = \frac{1}{2} \left( m \dot{q}_1^2 + 2m \cdot \dot{q}_2^2 \right)$$

$$M = \begin{bmatrix} 1 & 0 \\ 0 & 2 \end{bmatrix} m$$

$$D = \begin{bmatrix} \frac{1}{3} & \frac{2^3}{6} \\ \frac{2^3}{6} & \frac{20}{3} \end{bmatrix} \frac{l^3}{E}$$

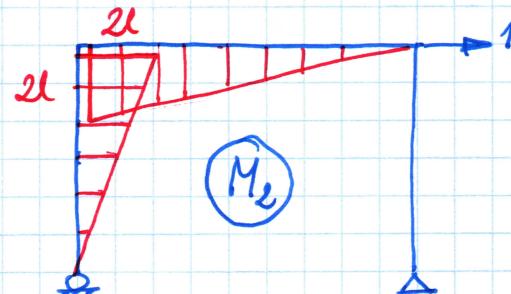
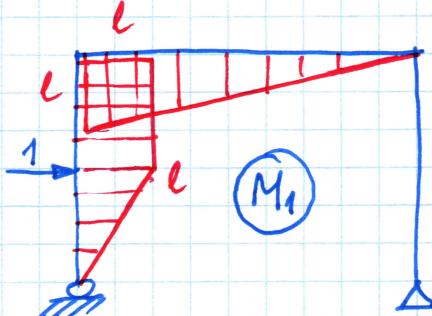
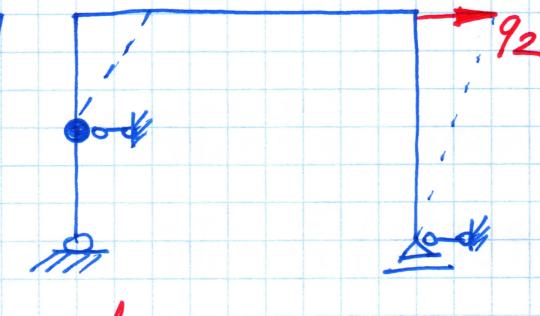
$$d_{f0} = \begin{bmatrix} \frac{2^3}{6} \\ \frac{20}{3} \end{bmatrix} \frac{l^3}{EJ}$$

$$(I - \theta^2 D M) q_f = d_{f0} P_0$$

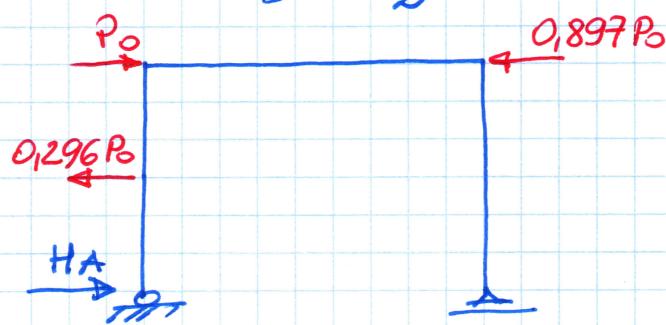
$$q_1 = -0,296 \frac{P_0 l^3}{EJ} \quad q_2 = -0,448 \frac{P_0 l^3}{EJ}$$

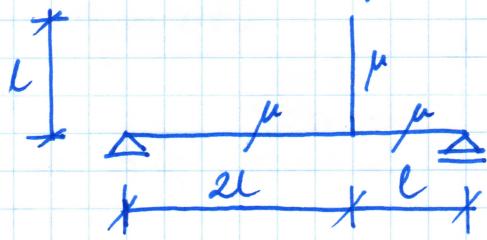
$$H_A = P_0 - 0,296 P_0 - 0,897 P_0 = 0$$

$$H_A = +0,193 P_0$$



$$M_3 = M_2$$

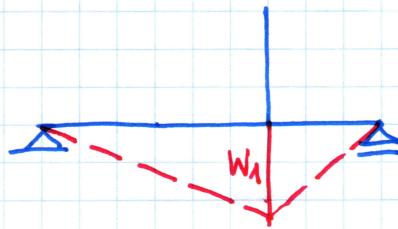
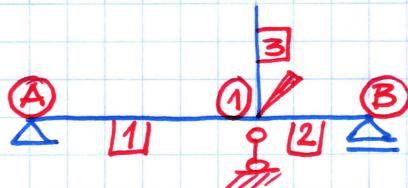




$$EJ = \text{const}$$

$$EA = \infty$$

$$\lambda_1 = 2\lambda \quad \lambda_3 = \lambda \\ \lambda_2 = \lambda$$



$$q_l = \begin{bmatrix} \varphi_1 \\ w_1 \\ \vdots \end{bmatrix}$$

Równania równowagi:

$$1) \varphi_1^1 + \varphi_1^2 + \varphi_1^3 = 0$$

$$2) W_1^1 \cdot \bar{w}_1 + W_1^2 \cdot \bar{w}_1 - B_{11}^{(3)}(-\bar{w}_1) = 0$$

$$B_{11}^{(3)} = -\mu l \cdot \omega^2 w_1$$

$$\varphi_1^1 = \frac{EJ}{2l} \left( \alpha'(2\lambda) \varphi_1 - \frac{1}{2} \theta'(2\lambda) \frac{w}{l} \right)$$

$$\varphi_1^2 = \frac{EJ}{l} \left( \alpha'(\lambda) \varphi_1 + \theta'(\lambda) \frac{w}{l} \right)$$

$$\varphi_1^3 = \frac{EJ}{l} (\alpha''(\lambda) \varphi_1)$$

$$W_1^1 = \frac{EJ}{4l^2} \left( -\theta'(2\lambda) \varphi_1 + \gamma'(2\lambda) \frac{w}{2l} \right)$$

$$W_1^2 = \frac{EJ}{l^2} \left( \theta'(\lambda) \varphi_1 + \gamma'(\lambda) \frac{w}{l} \right)$$

$$K(\lambda) = \frac{EJ}{l} \begin{bmatrix} \frac{1}{2} \alpha'(2\lambda) + \alpha''(\lambda) + \alpha'(\lambda) & - \frac{\theta'(2\lambda)}{4} + \theta'(\lambda) \\ - \frac{\theta'(2\lambda)}{4} + \theta'(\lambda) & \frac{\gamma'(2\lambda)}{8} + \gamma'(\lambda) - \lambda^4 \end{bmatrix}$$

$$\det(K(\lambda)) = 0 \rightarrow \omega_1$$